

FACTS 1 EQUITY PREMIUM AND RISK

	STOCKS REAL	BONDS REAL	STOCK- BOND	GDP	CONS- UMPTION	ND+S
E:	8.6	1.3	7.4	3.2	3.3	2.4
G:	17.6	2.6	18.1	2.6	2.1	2.0
CORR:	0.99	-0.03	1.00	0.32	0.39	0.43

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B14

EQUITY PREMIUM $E(R^{\text{Stock}} - R^{\text{BOND}}) \approx 7\%$ *RISK?*

B14

VOLATILITY OF STOCK RETURNS $\sigma(R^{\text{Stock}} - R^{\text{BOND}}) \approx 18\%$ *RIGHT MEASURE?*

STOCKS CORRELATED WITH ECONOMY

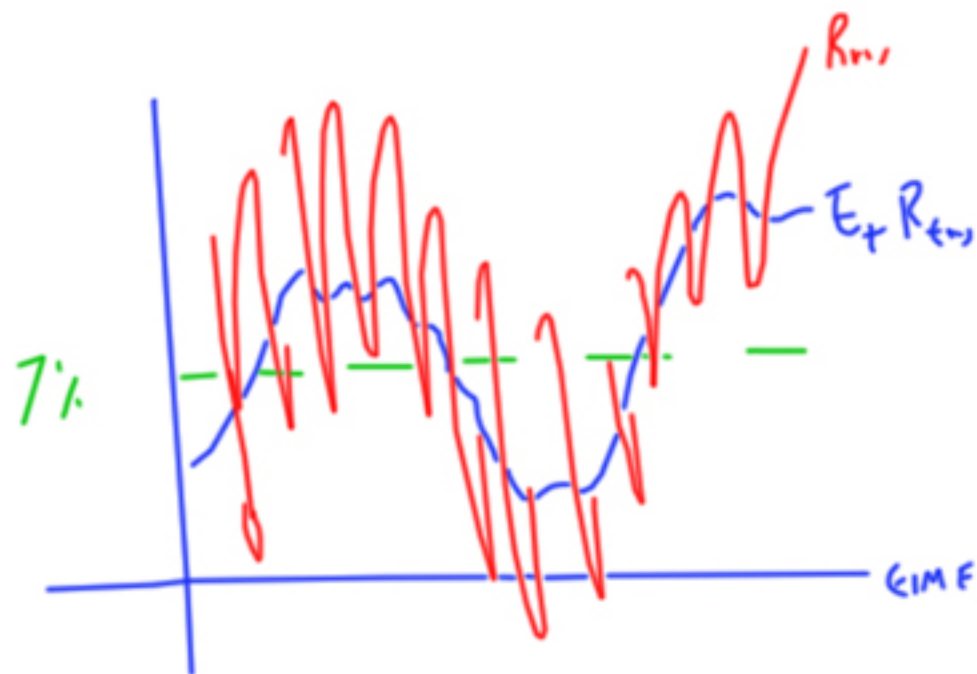
WHY SO RISKY?

FACTS 2: TIME VARYING RISK PREMIUM

$$R_{t+n} = a + b X_t + \epsilon_{t+n}$$

$$E_t R_{t+n} = \underline{a + b X_t}$$

$\underline{b=0} \rightarrow E_t R_{t+n} = \text{CONST.}$



$\frac{P_t}{D_t}$ FORECASTS RETURNS

$E_t(R_{t+n})$ IS BIG; VARIES A LOT OVERTIME
BIG IN RECESSIONS

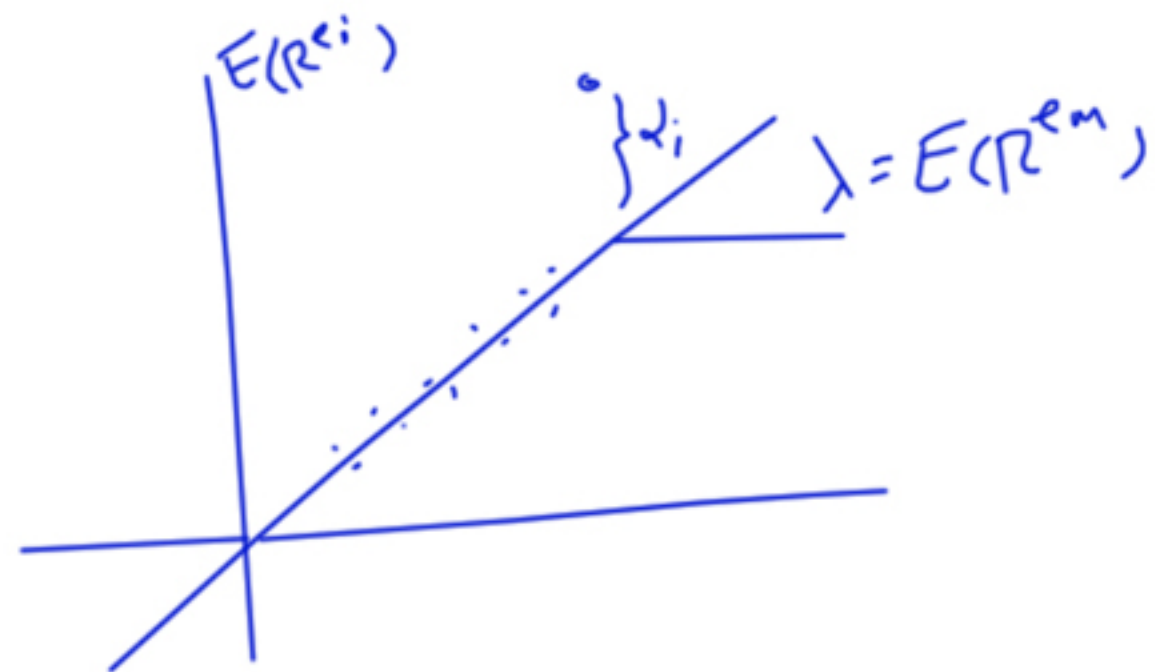
$\frac{P_t}{D_t}$ DOES NOT FORECAST D !

$P_t = E[\underline{\underline{\text{DISCOUNTED DIV.}}}]$

FACTS 3: THE CROSS SECTION OF STOCK RETURNS

CAPM

$$E(R^{e_i}) = [\alpha_i] + \beta_i E(R^{e_M})$$



F3F

$$E(R^{e_i}) = [\alpha_i] + b_i E(r_{MRF}) + h_i E(hml) + S_i E(smb)$$

WHY?

WHY $E(R^{e_M})$; WHY $E(hml)$?

"MODEL OF RETURNS" - FACTORS

FACTS SUMMARY

RISK PREMIUM
EXPECTED RETURN

1) $E(R^e)$ IS BIG! 7% → **BUY? RISK?**

$\sigma(R^e)$ IS BIG, 18%.

R^e IS CORRELATED WITH $\Delta C, \Delta Y$ **STOCKS FALL IN BAD TIMES**

2) $E_t(R_{t+n}^e)$ VARIABLES OVER TIME $\sigma[E_t(R_{t+n}^e)] \approx 6\%$!

→ **BUY! TIME VARYING RISK PREMIUM?**

3) $E_t(R_{t+n}^{e_i})$ VARIABLES ACROSS ASSETS A LOT!

FACTOR MODELS

WHY ARE "FACTORS PRICED" PREMIUM FOR VALUE-GROWTH

THEORY OVERVIEW. PREVIEW

• WHATS IT WORTH? TIME AND RISK

• dV/dx RISK MANAGEMENT



• INVESTMENT VS EQUILIBRIUM

• WHAT DOES THE MARKET LOOK LIKE
AFTER INVESTMENT?

GOAL
$$P_c = E_x \left(\beta \frac{V'(C_{t+1})}{V'(C_t)} X_{t+1} \right)$$

$$P = E(mX)$$

ALL CLASSIC ISSUES OF FINANCE. I

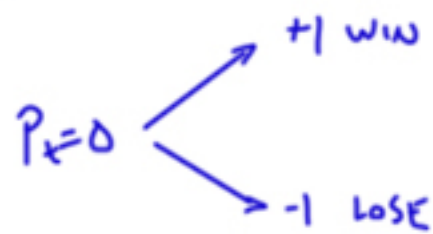
THEORY OVERVIEW: X AND U TO P = E(MX)

PAYOFF
X

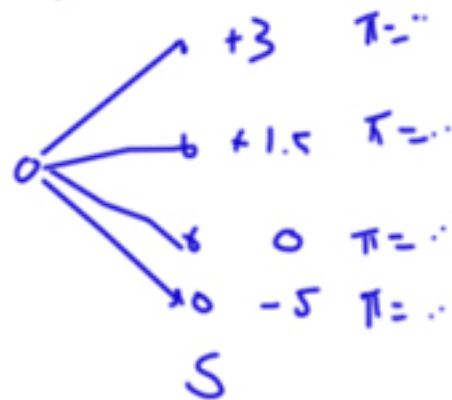
Stock: $P_t \rightarrow X_{t+1} = P_{t+1} + d_{t+1}$

BOND: $P_t \rightarrow 1$
 $1 \rightarrow R^f$

BET:



X_{t+1} IS RANDOM



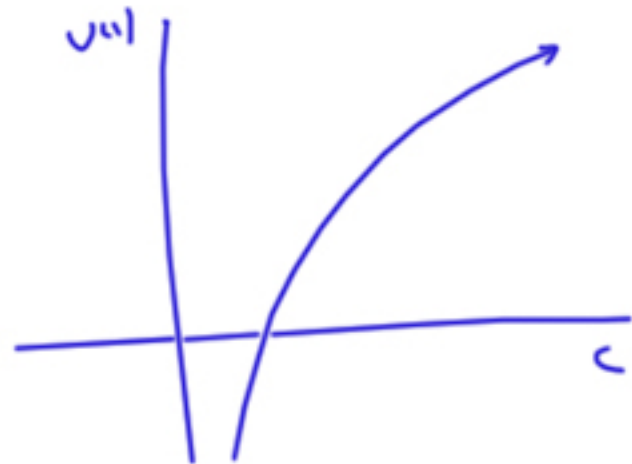
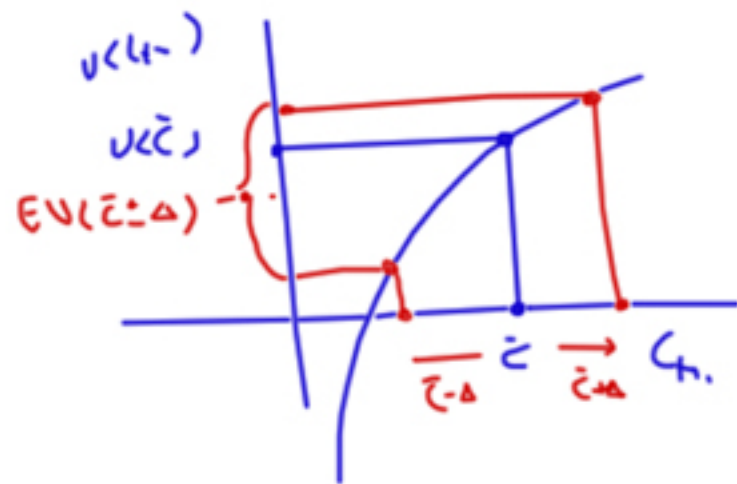
UTILITY

$X \rightarrow P?$

VALUE TO WHO?

$$U(c_t, c_{t+1}) = U(c_t) + \beta E_t [U(c_{t+1})]$$

discount factor \rightarrow TIME



$$V(C) = \frac{C^{1-\gamma} - 1}{1-\gamma} \quad \underline{U'(C) = C^{-\gamma}}$$

$$\gamma \rightarrow 1 \quad V(C) = \log(C)$$

$$\text{MAX}_C \quad V(C_t - P_t) + \beta E_t V(C_{t+1} + X_{t+1})$$

$$P_t U'(C_t) = \beta E_t (U'(C_{t+1}) \cdot X_{t+1})$$

$$P_t = E_t \left[\underbrace{\beta \frac{U'(C_{t+1})}{U'(C_t)}}_{M_{t+1}} X_{t+1} \right] = E_t \left[\beta \left(\frac{C_{t+1}}{C_t} \right)^{-\gamma} X_{t+1} \right]$$

• AFTER INVESTMENT

• YOUR \leq ADJUSTS

• MARGINAL

$$P_t = E_t (X_{t+1})?$$

$$P_t = E_t \left(\frac{1}{R} X_{t+1} \right)^?$$

$\underbrace{\quad}_{0.9}$

$$P_t = E_t (M_{t+1} X_{t+1})$$

↑
RANDOM,
STOCHASTIC

